Topic 12:

Sequences and Strings

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Sequences	
Definition: Sequence [1st Attempt]	
Notation:	
inotation.	
Example(s):	

Rules

Recall:	$\sum_{i=1}^{n} 2i$		
Example(s):	i=1		
Two Notations	for Infinite Sequence	es:	
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Sequences	s and Function	IS	
	s and Function equence [Final Version]		
Definition: Se			
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Arithmetic and Geometric Sequences

Definition: Arithmetic Sequence (a.k.a. Arithmetic Progression)

Definition: Geometric Sequence (a.k.a. Geometric Progression)

Example(s):

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Arithmetic Series

The sum of the terms of an arithmetic sequence (a.k.a.

arithmetic series): $s_n = a_1 + \ldots + a_n = \frac{1}{2}n(a_1 + a_n)$

Here's why: First, note that $a_n = a_1 + (n-1)d$.

Next, here are two expressions for s_n :

$$s_n = a_1 + (a_1 + d) + (a_1 + 2d) + \dots + (a_1 + (n-1)d)$$

$$s_n = (a_n - (n-1)d) + (a_n - (n-2)d) + \dots + (a_n - d) + a_n$$

Sum these expressions, and the d terms cancel, leaving:

$$2s_n = na_1 + na_n$$
, or $s_n = \frac{1}{2}n(a_1 + a_n)$.

Increasing Sequences

Definition: Increasing Sequence	
Definition: Non-Decreasing Sequence	
Definition: Strictly Increasing Sequence	
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Decreasing Sequences	
Definition: Decreasing Sequence	
Definition: Non-Increasing Sequence	
Definition: Strictly Decreasing Sequence	

Examples: Increasing/Decreasing Sequences

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Subsequences	
Definition: Subsequence	
Example(s):	

Need to Identify a Sequence?

A great resource for sequences:	
The Online Encyclopedia of Integer Sequences	

(http://oeis.org/)

Example(s):	
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Strings (1 / 2)	Somewhat beyond the programming language kind
Definition: String	
Example(s):	

Strings (2 / 2)

Notation:

- Lambda (λ) represents the empty (null) string
- ullet xy means strings x and y are concatenated
- Superscripts denote repetition of concatenation
- |x| represents the length of string x
- A^* is the set of strings that can be formed using elements of an alphabet A.
 - $\circ A^*$ is an infinite set
 - $\circ \lambda \in A^*$

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Set Cardinality Revisited (1 / 5)

An observation about set cardinality:

Definition: Finite

Set Cardinality Revisited (2 / 5)

Definition: Countably Infinite (a.k.a. Denumerably	y Infinite)
Definition: Countable	
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Set Cardinality Revisited (3 / 5)	
Example(s):	

Set Cardinality Revisited (4 / 5)

Question. Are the positive rati	onal numbers countable?
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Set Cardinality Revisite	ed (5 / 5)
Set Cardinality Revisite Conjecture: A pairing function	
Set Cardinality Revisite Conjecture: A pairing function	

Now You Can Understand More Cartoons! (1/2)

Background: Elephant jokes became popular form of absurdist humor in the U.S. in the 1960s. For example:

Q: How many elephants can fit in a Jeep?

A: Four – Two in the front and two in the back.

Q: How many bison can fit in a Jeep?

A: None – it's full of elephants.

Q: How do you know when there are two elephants in your closet?

A: You hear giggling when the door is closed.

Q: How do you know when there are three elephants in your closet?

A: You can't close the door.

Q: How do you know when there are four elephants in your closet?

A: There's an empty Jeep in the driveway.

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Now You Can Understand More Cartoons! (2/2)







http://www.userfriendly.org/cartoons/archives/05jun/uf008006.gif