

# CSc 110, Autumn 2016

## Lecture 10: Advanced `if/else`; Cumulative sum

Adapted from slides by Marty Stepp and Stuart Reges

### BOOLEAN HAIR LOGIC

A



B



AND



OR



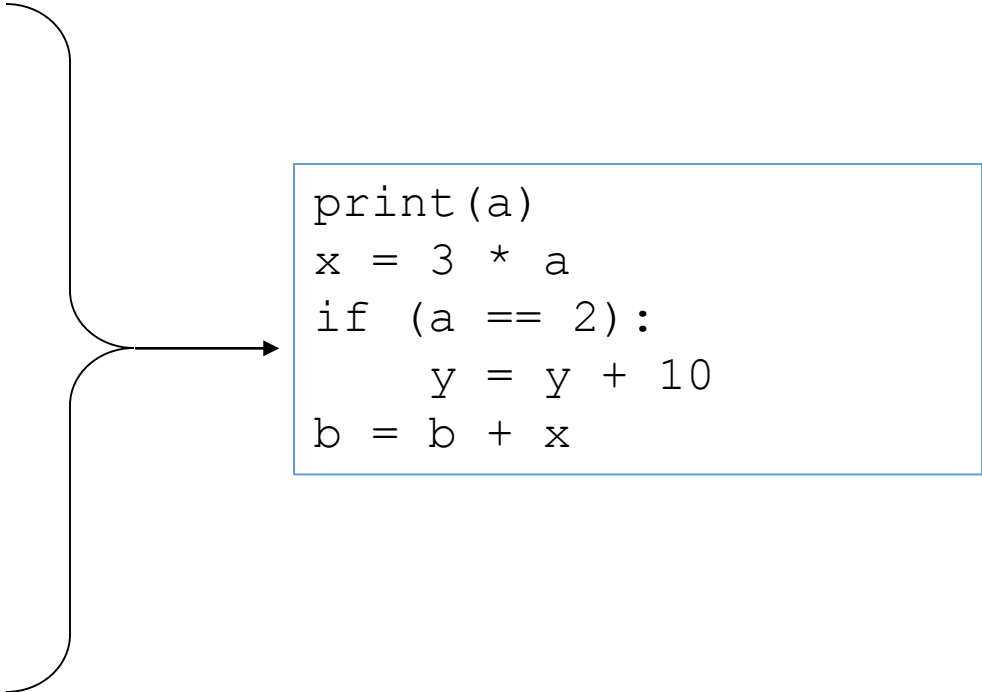
XOR

# Factoring `if/else` code

- **factoring:** Extracting common/redundant code.
  - Can reduce or eliminate redundancy from `if/else` code.

- **Example:**

```
if (a == 1):
    print(a)
    x = 3
    b = b + x
elif (a == 2):
    print(a)
    x = 6
    y = y + 10
    b = b + x
else:           # a == 3
    print(a)
    x = 9
    b = b + x
```



```
print(a)
x = 3 * a
if (a == 2):
    y = y + 10
b = b + x
```

# Relational expressions

- `if` statements use logical tests.

```
if (i <= 10) { ...
```

- These are `boolean` expressions.
- Tests use *relational operators*:

Operator	Meaning	Example	Value
<code>==</code>	equals	<code>1 + 1 == 2</code>	true
<code>!=</code>	does not equal	<code>3.2 != 2.5</code>	true
<code>&lt;&gt;</code>		<code>3.2 &lt;&gt; 2.5</code>	
<code>&lt;</code>	less than	<code>10 &lt; 5</code>	false
<code>&gt;</code>	greater than	<code>10 &gt; 5</code>	true
<code>&lt;=</code>	less than or equal to	<code>126 &lt;= 100</code>	false
<code>&gt;=</code>	greater than or equal to	<code>5.0 &gt;= 5.0</code>	true

# Logical operators

- Tests can be combined using *logical operators*:

<b>Operator</b>	<b>Description</b>	<b>Example</b>	<b>Result</b>
and	and	<code>(2 == 3) and (-1 &lt; 5)</code>	False
or	or	<code>(2 == 3) or (-1 &lt; 5)</code>	True
not	not	<code>not (2 == 3)</code>	True

- "Truth tables" for each, used with logical values  $p$  and  $q$ :

<b>P</b>	<b>q</b>	<b>p and q</b>	<b>p or q</b>
True	True	True	True
True	False	False	True
False	True	False	True
False	False	False	False

<b>p</b>	<b>not p</b>
True	False
False	True

# Evaluating logical expressions

- Relational operators have lower precedence than math; logical operators have lower precedence than relational operators

`5 * 7 >= 3 + 5 * (7 - 1) and 7 <= 11`

`5 * 7 >= 3 + 5 * 6 and 7 <= 11`

`35 >= 3 + 30 and 7 <= 11`

`35 >= 33 and 7 <= 11`

`True and True`

`True`

- Relational operators cannot be "chained" as in algebra

`2 <= x <= 10`

`True <= 10` (assume that x is 15)

- Instead, combine multiple tests with `and` or `or`

`2 <= x and x <= 10`

`True and False`

`False`

# Logical questions

- What is the result of each of the following expressions?

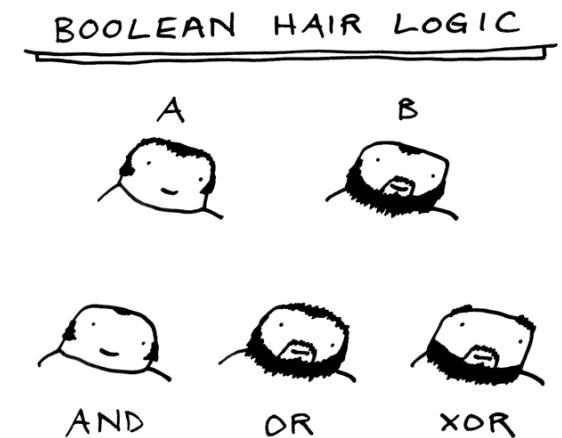
$x = 42$

$y = 17$

$z = 25$

- $y < x$  and  $y \leq z$
- $x \% 2 == y \% 2$  or  $x \% 2 == z \% 2$
- $x \leq y + z$  and  $x \geq y + z$
- $\text{not}(x < y \text{ and } x < z)$
- $(x + y) \% 2 == 0$  or  $\text{not}((z - y) \% 2 == 0)$

- **Answers:** True, False, True, True, False



# Cumulative algorithms

# Adding many numbers

- How would you find the sum of all integers from 1-1000?

```
# This may require a lot of typing
```

```
sum = 1 + 2 + 3 + 4 + ...
```

```
print("The sum is " + str(sum))
```

- What if we want the sum from 1 - 1,000,000?  
Or the sum up to any maximum?
  - How can we generalize the above code?



# Cumulative sum loop

```
sum = 0
for i in range(1, 1001):
    sum = sum + i

print("The sum is " + str(sum))
```

- **cumulative sum:** A variable that keeps a sum in progress and is updated repeatedly until summing is finished.
  - The `sum` in the above code is an attempt at a cumulative sum.
  - Cumulative sum variables must be declared *outside* the loops that update them, so that they will still exist after the loop.

# Cumulative product

- This cumulative idea can be used with other operators:

```
product = 1  
for i in range(1, 21):  
    product = product * 2  
  
print("2 ^ 20 = " + str(product))
```

- How would we make the base and exponent adjustable?

# input and cumulative sum

- We can do a cumulative sum of user input:

```
sum = 0;
for i in range(1, 101):
    next = int(input("Type a number: "))
    sum = sum + next
}
print("The sum is " + str(sum))
```

# Cumulative sum question

- Modify the `Receipt` program from lecture 2
  - Prompt for how many people, and each person's dinner cost.
  - Use functions to structure the solution.
- Example log of execution:

```
How many people ate? 4
Person #1: How much did your dinner cost? 20.00
Person #2: How much did your dinner cost? 15
Person #3: How much did your dinner cost? 30.0
Person #4: How much did your dinner cost? 10.00
```

```
Subtotal: $75.0
Tax: $6.0
Tip: $11.25
Total: $92.25
```

# Cumulative sum answer

```
# This program enhances our Receipt program using a cumulative sum.
```

```
def main():
```

```
    subtotal = meals()
```

```
    results(subtotal)
```

```
# Prompts for number of people and returns total meal subtotal.
```

```
def meals():
```

```
    people = float(input("How many people ate? "))
```

```
    subtotal = 0.0;                # cumulative sum
```

```
    for i in range(1, people + 1):
```

```
        person_cost = float(input("Person #" + str(i) +  
                                   ": How much did your dinner cost? "))
```

```
        subtotal = subtotal + person_cost; # add to sum
```

```
    return subtotal
```

```
...
```

# Cumulative answer, cont'd.

```
# Calculates total owed, assuming 8% tax and 15% tip
```

```
def results(subtotal):  
    tax = subtotal * .08  
    tip = subtotal * .15  
    total = subtotal + tax + tip  
  
    print("Subtotal: $" + str(subtotal))  
    print("Tax: $" + str(tax))  
    print("Tip: $" + str(tip))  
    print("Total: $" + str(total))
```

# if/else, return question

- Write a function `count_factors` that returns the number of factors of an integer.
  - `count_factors(24)` returns 8 because 1, 2, 3, 4, 6, 8, 12, and 24 are factors of 24.

- Solution:

```
# Returns how many factors the given number has.  
def count_factors(number):  
    count = 0  
    for i in range(1, number + 1):  
        if (number % i == 0):  
            count += 1          # i is a factor of number  
    return count
```