Prolog Types

- The term is Prolog’s basic data structure.
- Everything is expressed in the form of a term. This includes programs and data.
- Prolog has four basic types of terms:
  - variables start with an uppercase letter;
  - compound terms are lists, strings, and structures;
  - atoms start with a lower-case letter;
  - numbers.

Prolog Numbers

- Most Prolog implementations support infinite precision integers. This is not true of GNU Prolog!
- The built-in operator \texttt{is} evaluates arithmetic expressions:
  \begin{verbatim}
  | ?- X is 6*7.  
  X = 42 
  | ?- X is 6.0*7.0. 
  X = 42.0 
  | ?- X is 60000000000000*7000000000000000. 
  X = 1
  \end{verbatim}
Prolog Arithmetic Expressions

- An *infix* expression is just shorthand for a **structure**:
  
  ```prolog
  | ?- X = +(1,*((2,3)).
  X = 1+2*3
  | ?- X = 1+2*3.
  X = 1+2*3
  | ?- X is +(1,*((2,3)).
  X = 7
  | ?- X is 1+2*3.
  X = 7
  
  X = 1*2 means “make the variable X and 1*2 the same”. It looks like an assignment, but it’s what we call **unification**. More about that later.
  
Prolog Atoms

- **Atoms** are similar to enums in C.
  
  - Atoms start with a lower-case letter and can contain letters, digits, and underscore (_).

  ```prolog
  | ?- X = hello.
  X = hello
  | ?- X = hE_l_l_o99.
  X = hE_l_l_o99
  
Prolog Variables

- **Variables** start out **uninstantiated**, i.e. without a value.

  - Uninstantiated variables are written **_number**:

    ```prolog
    | ?- write(X).
    _16
    
  
  - Once a Prolog variable has been **instantiated** (given a value), it will keep that value.

    ```prolog
    | ?- X=sally.
    X = sally
    | ?- X=sally, X=lisa.
    no
    
    ```prolog
    | ?- (X=sally; X=lisa), write(X), nl.
    sally
    X = sally ? ;
    lisa
    X = lisa
    ```
Prolog Programs

- A Prolog program consists of a database of **facts** and **rules**:
  - `likes(lisa, chocolate).
  - `likes(lisa, X) :- tastes_like_chocolate(X).``
- `:-` is read as `if`.
- `:-` is just an operator, like other Prolog operators. The following are equivalent:
  - `likes(lisa, X) :- boy(X), tastes_like_chocolate(X).``
- `(likes(lisa, X),
  (boy(X), tastes_like_choc(X))).``

Prolog Programs...

- Prolog facts/rules can be **overloaded**, wrt their **arity**.
- You can have a both a rule `foo()` and a rule `foo(X):
  - `?- [user].
  - foo.
  - foo(hello).
  - foo(bar, world).
  - foo(X, Y, Z) :-
    Z is X + Y.
<ctrl-D>``
  - `?- foo.
  - yes
  - `?- foo(X).
    X = hello
  - `?- foo(X, Y).
    X = bar
    Y = world
  - `?- foo(1, 2, Z).
    Z = 3``

Standard predicates

- `read(X)` and `write(X)` read and write Prolog terms.
- `nl` prints a newline character.
  - `?- read(X), write(X), nl.
    hello.
    hello``

Standard predicates...

- `write` can write arbitrary Prolog terms:
  - `?- write(hello(world)), nl.
    hello(world)``
- Note that `read(X)` requires the input to be syntactically correct and to end with a period.
  - `?- read(X).
    foo).
    uncaught exception: error`
Unification/Matching

- The `=`-operator tries to make its left and right-hand sides the same.
- This is called unification or matching.
- If Prolog can’t make \( X \) and \( Y \) the same in \( X = Y \), matching will fail.

<table>
<thead>
<tr>
<th>X = lisa, Y = sally, X = Y.</th>
</tr>
</thead>
<tbody>
<tr>
<td>no</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>X = lisa, Y = lisa, Z = X, Z = Y.</th>
</tr>
</thead>
<tbody>
<tr>
<td>X = lisa</td>
</tr>
<tr>
<td>Y = lisa</td>
</tr>
<tr>
<td>Z = lisa</td>
</tr>
</tbody>
</table>

- We will talk about this much more later.

Backtracking

- Prolog will try every possible way to satisfy a query.
- Prolog explores the search space by using backtracking, which means undoing previous computations, and exploring a different search path.

Māori Family Relationships

- Here’s an example:

<table>
<thead>
<tr>
<th>X = lisa, Y = sally; X = lisa, Y = sally, pretty(X).</th>
</tr>
</thead>
<tbody>
<tr>
<td>X = lisa</td>
</tr>
</tbody>
</table>

- We will talk about this much more later.

John Foster (in *He Whakamaarama – A New Course in Māori*) writes:

*Relationship is very important to the Māori. Social seniority is claimed by those able to trace their whakapapa or genealogy in the most direct way to illustrious ancestors. Rights to shares in land and entitlement to speak on the marae may also depend on relationship. Because of this, there are special words to indicate elder or younger relations, or senior or younger branches of a family.*

- Māori is the indigenous language spoken in New Zealand. It is a polynesian language, and closely related to the language spoken in Hawaii.
A program to translate between English and Māori must take into account the differences in terms of address between the two languages.

Write a Prolog predicate `calls(X,Y,Z)` which, given a database of family relationships, returns all the words that X can use to address or talk about Y.

?- calls(aanaru, hata, Z). Z = tuakana ; Z = maataamua ; no

?- calls(aanaru, rapeta, Z). Z = teina ; no

Literally: "What you follow at night"
The Whanau Program — Database Facts

- We start by encoding the family as facts in the Prolog database.

% person(name, sex, father, mother, spouse, birth-year).

person(hoone, male, unknown, unknown, rita, 1910).
person(rita, female, unknown, unknown, hoone, 1915).
person(ranginui, male, unknown, unknown, ranginui, 1915).
person(meroana, female, unknown, unknown, rangoana, 1916).
person(rewi, male, hoone, rita, 1935).
person(rahia, female, ranginui, rangoana, rita, 1916).
person(hata, male, rewi, rahia, none, 1957).
person(kiri, female, rewi, rahia, none, 1959).

% person(name, sex, father, mother, spouse, birth-year).

person(hiniera, female, rewi, rahia, pita, 1960).
person(anaru, male, rewi, rahia, none, 1962).
person(rapeta, male, rewi, rahia, none, 1964).
person(mere, female, rewi, rahia, none, 1965).
person(pita, male, unknown, unknown, hiniera, 1960).
person(moeraa, female, pita, hiniera, none, 1986).
person(huia, female, pita, hiniera, none, 1987).
person(irihaapeti, female, pita, hiniera, none, 1988).

---

- Whanau is Māori for family.
- Below is a table showing an extended Māori family.

<table>
<thead>
<tr>
<th>Name</th>
<th>Sex</th>
<th>Father</th>
<th>Mother</th>
<th>Spouse</th>
<th>Born</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hoone</td>
<td>male</td>
<td>unknown</td>
<td>unknown</td>
<td>Rita</td>
<td>1910</td>
</tr>
<tr>
<td>Rita</td>
<td>female</td>
<td>unknown</td>
<td>unknown</td>
<td>Hone</td>
<td>1915</td>
</tr>
<tr>
<td>Ranginui</td>
<td>male</td>
<td>unknown</td>
<td>unknown</td>
<td>Rangoana</td>
<td>1915</td>
</tr>
<tr>
<td>Rangoana</td>
<td>female</td>
<td>unknown</td>
<td>unknown</td>
<td>Rangoana</td>
<td>1916</td>
</tr>
<tr>
<td>Rewi</td>
<td>male</td>
<td>Hoone</td>
<td>Rita</td>
<td>Rahia</td>
<td>1935</td>
</tr>
<tr>
<td>Rahia</td>
<td>female</td>
<td>Rangoana</td>
<td>Rangoana</td>
<td>Rewi</td>
<td>1940</td>
</tr>
<tr>
<td>Hata</td>
<td>male</td>
<td>Rewi</td>
<td>Rahia</td>
<td>none</td>
<td>1957</td>
</tr>
<tr>
<td>Kiri</td>
<td>female</td>
<td>Rewi</td>
<td>Rahia</td>
<td>none</td>
<td>1959</td>
</tr>
<tr>
<td>Hiniera</td>
<td>female</td>
<td>Rewi</td>
<td>Rahia</td>
<td>Pita</td>
<td>1960</td>
</tr>
<tr>
<td>Anaru</td>
<td>male</td>
<td>Rewi</td>
<td>Rahia</td>
<td>none</td>
<td>1962</td>
</tr>
<tr>
<td>Rapeta</td>
<td>male</td>
<td>Rewi</td>
<td>Rahia</td>
<td>none</td>
<td>1964</td>
</tr>
<tr>
<td>Mere</td>
<td>female</td>
<td>Rewi</td>
<td>Rahia</td>
<td>none</td>
<td>1965</td>
</tr>
<tr>
<td>Pita</td>
<td>male</td>
<td>unknown</td>
<td>unknown</td>
<td>Hiniera</td>
<td>1960</td>
</tr>
<tr>
<td>Moeraa</td>
<td>female</td>
<td>Pita</td>
<td>Hiniera</td>
<td>none</td>
<td>1986</td>
</tr>
<tr>
<td>Huia</td>
<td>female</td>
<td>Pita</td>
<td>Hiniera</td>
<td>none</td>
<td>1987</td>
</tr>
<tr>
<td>Irihaapeti</td>
<td>female</td>
<td>Pita</td>
<td>Hiniera</td>
<td>none</td>
<td>1988</td>
</tr>
</tbody>
</table>
We introduce some auxiliary predicates to extract information from the database.

Auxiliary predicates:
- gender(X, G) :- person(X, G, _, _, _, _).
- othergender(male, female).
- othergender(female, male).
- female(X) :- gender(X, female).
- male(X) :- gender(X, male).

We next write some predicates that compute common family relationships.

% Is Y the <operator> of X?
- wife(X, Y) :- person(X, male, _, _, Y, _).
- husband(X, Y) :- person(X, female, _, _, Y, _).
- spouse(X, Y) :- wife(X, Y).
- spouse(X, Y) :- husband(X, Y).
- parent(X, Y) :- person(X, _, Y, _, _, _).
- parent(X, Y) :- person(X, _, _, Y, _, _).
- son(X, Y) :- person(Y, male, X, _, _, _).
- son(X, Y) :- person(Y, male, _, X, _, _).
- daughter(X, Y) :- person(Y, female, X, _, _, _).
- daughter(X, Y) :- person(Y, female, _, X, _, _).
- child(X, Y) :- son(X, Y).
- child(X, Y) :- daughter(X, Y).

Some of the following are left as an exercise:

% Is X older than Y?
older(X, Y) :-
  person(X, _, _, _, _, Xyear),
  person(Y, _, _, _, _, Yyear),
  Yyear > Xyear.

% Is Y a sibling of X of the gender G?
sibling(X, Y, G) :- <left as an exercise>.

% Is Y one of X's older siblings of gender G?
oldersibling(X, Y, G) :- <left as an exercise>.

% Is Y one of X's older/younger siblings of either gender?
oldersibling(X, Y) :- <left as an exercise>.

% Is Y an ancestor of X of gender G?
ancestor(X, Y, G) :- <left as an exercise>.

% Is Y an older relative of X of gender G?
olderrelative(X, Y, G) :-
  ancestor(X, Y, G).

% Is Y a sibling of X of his/her opposite gender?
siblingofothersex(X, Y) :- <left as an exercise>. 
We can now finally write the predicate \texttt{calls(X,Y,T)} which computes all the ways \( T \) in which \( X \) can address \( Y \).

\begin{verbatim}
% Me.
calls(X, X, au).

% Parents.
calls(X,Y,paapaa) :- person(X, _,Y, _, _, _).
calls(X,Y,maamaa) :- person(X, _, _,Y, _, _).

% Oldest/youngest sibling of same sex.
calls(X, Y, tuakana) :-
    gender(X, G), eldestsibling(X, Y, G).
calls(X, Y, teina) :-
    gender(X, G), youngestsibling(X, Y, G).
\end{verbatim}

% Siblings of other sex.
calls(X, Y, tungaane) :- <left as an exercise>.
calls(X, Y, tuahine) :- <left as an exercise>.
calls(X, Y, tipuna) :- <left as an exercise>.

% Sons and daughters.
calls(X, Y, tama) :- <left as an exercise>.
calls(X, Y, tamahine) :- <left as an exercise>.

% Oldest/youngest child.
calls(X, Y, maataamua) :- <left as an exercise>.
calls(X, Y, pootiki) :- <left as an exercise>.

% Child-in-law.
calls(X, Y, hunaonga) :- <left as an exercise>.

% Grandchild.
calls(X, Y, mokopuna) :- <left as an exercise>.

---

**Summary**

- Read *Clocksin-Mellish, Chapter 2*. 
Prolog terms:
- atoms (a, 1, 3.14)
- structures
  - guitar(ovation, 1111, 1975)

Infix expressions are abbreviations of "normal" Prolog terms:

<table>
<thead>
<tr>
<th>infix</th>
<th>prefix</th>
</tr>
</thead>
<tbody>
<tr>
<td>a + b</td>
<td>+(a, b)</td>
</tr>
<tr>
<td>a + b * c</td>
<td>+(a, *(b, c))</td>
</tr>
</tbody>
</table>