# CSc 520 — Principles of Programming Languages

40: Scheme — Metacircular Interpretation

Christian Collberg
Department of Computer Science
University of Arizona
collberg+520@gmail.com

Copyright © 2008 Christian Collberg

May 2, 2008

#### 1 Introduction

- In this lecture I'm going to show how you can define Scheme by writing a *metacircular interpreter* for the language, i.e. an interpreter for Scheme written in Scheme.
- Before we can do that, we first need to learn a few more this about the language

## 2 Let Expressions

• A let-expression binds names to values:

• The first argument to let is a list of (name value) pairs. The second argument is the expression to evaluate.

## 3 Let Expressions...

• Let-expressions can be nested:

28

### 4 Imperative Features

- Scheme is an *impure* functional language.
- I.e., Scheme has *imperative* features.
- I.e., in Scheme it is possible to program with side-effects.

(set! var value) Change the value of var to value.

(set-car! var value) Change the car-field of the cons-cell var to value.

(set-cdr! var value) Change the cdr-field of the cons-cell var to value.

## 5 Imperative Features...

• Example:

#### 6 Dotted Pairs

- S-expressions are constructed using dotted pairs.
- It is implemented as a struct (called a *cons-cell*) consisting of two fields (the size of a machine word) called car and cdr.
- We can manipulate these fields directly:

#### 7 Dotted Pairs...

• When the second part of a dottend pair (the cdr-field) is a list, and the innermost cdr-field is the empty list, we get a "normal" Scheme list:

#### 8 Dotted Pairs...

• We can use set-car! and set-cdr! to manipulate the fields of a cons-cell directly:

```
> (define x '(1 . 2))
> (set-car! x 'a)
> x
(a . 2)
> (set-cdr! x '(2 3))
> x
(a 2 3)
```

#### 9 Dotted Pairs...

• (cons A B) can be thought of as first creating a cons-cell on the heap (using malloc, for example), and then setting the car and cdr fields to A and B, respectively:

```
> (define x (cons 0 0))
> x
(0 . 0)
> (set-car! x '1)
> (set-cdr! x '())
> x
(1)
```

### 10 Loops

Scheme's "for-loop" do takes these arguments:

- 1. A list of triples (var init update) which declares a variable var, with an initial value init, and which gets updated using the expression update, on each iteration;
- 2. A pair (termination\_cond return\_value) which gives the termination condition and return value of the loop; and
- 3. a loop body:

## 11 Loops...

• Sum the numbers 1 to 4, printing out intermediate results:

#### 12 Association Lists

• Association lists are simply lists of key-value pairs that can be searched sequentially:

• The list is searchedy the list from beginning to end, returning the first pair with a matching key:

(assoc key alist) Search for key; compare using equal?.

(assq key alist) Search for key; compare using eq?.

(assv key alist) Search for key; compare using eqv?.

#### 13 Association Lists...

```
> (define e '((a 1) (b 2) (c 3)))
> (assq 'a e)
(a 1)
> (assq 'b e)
(b 2)
> (assq 'd e)
#f
> (assq (list 'a) '(((a)) ((b)) ((c))))
#f
> (assoc (list 'a) '(((a)) ((b)) ((c))))
((a))
> (assv 5 '((2 3) (5 7) (11 13)))
(5 7)
```

#### 14 Association Lists...

• We can actually have more than one value:

### 15 Apply

• Apply returns the result of applying its first argument to its second argument.

#### 16 Eval

• (eval arg) evaluates its argument.

#### 17 Eval...

• eval and quote are each other's inverses:

## 18 Programs as Data

- Scheme is *homoiconic*, self-representing, i.e. programs and data are both represented the same (as S-expressions).
- This allows us to write programs that generate programs useful in AI, for example.

#### 19 Evaluation Order

- So far, we have said that to evaluate an expression (op arg1 arg2 arg3) we first evaluate the arguments, then apply the operator op to the resulting values.
- This is known as applicative-order evaluation.
- Example:

```
(define (double x) (* x x))

> (double (* 3 4))

⇒ (double 12)

⇒ \frac{(+ 12 12)}{+ 24}

⇒ 24
```

#### 20 Evaluation Order...

- This is not the only possible order of evaluation
- In normal-order evaluation parameters to a function are always passed unevaluated.
- This sometimes leads to extra work:

$$\frac{\text{(define (double x) (* x x))}}{\Rightarrow \frac{(+ (* 3 4) (* 3 4)))}{\Rightarrow \frac{(+ 12 (* 3 4))}{(+ 12 12)}}}$$

$$\Rightarrow \frac{(+ 12 12)}{\Rightarrow 24}$$

#### 21 Evaluation Order...

• Applicative-order can sometimes also lead to more work than normal-order:

$$\frac{\text{(define (switch x a b c)}}{\frac{\text{(cond}}{\frac{\text{((< x 0) a)}}{\frac{\text{((= x 0) b)}}{\text{((> x 0) c)))}}}}$$
> (switch -1 (+ 1 2) (+ 2 3) (+ 3 4))

• Here, applicative-order evaluates all the arguments, although only one value will ever be needed.

#### 22 Evaluation Order...

- Ordinary Scheme functions (such as +, car, etc) use applicative-order evaluation.
- Some *special forms* (cond, if, etc) must use normal order since they need to consume their arguments unevaluated:

### 23 A Metacircular Interpreter

- One way to define the semantics of a language (the effects that programs written in the language will have), is to write a metacircular interpreter.
- I.e, we define the language by writing an interpreter for it, in the language itself.
- A metacircular interpreter for Scheme consists of two mutually recursive functions, mEval and mApply:

```
(define (mEval Expr)
    ...
)
(define (mApply Op Args)
    ...
)
```

### 24 A Metacircular Interpreter...

• We want to be able to call our interpreter like this:

```
> (mEval (+ 1 2))
3
> (mEval (+ 1 (* 3 4)))
13
> (mEval (quote (2 3)))
(2 3)
> (mEval (car (quote (1 2))))
1
```

## 25 A Metacircular Interpreter...

```
> (mEval (cdr (quote (1 2))))
(2)
> (mEval (cons (quote 5) (quote (1 2))))
(5 1 2)
> (mEval (null? (quote (1 2))))
#f
> (mEval (null? (quote ())))
#t
> (mEval (if (eq? 1 1) 5 6))
5
```

## 26 A Metacircular Interpreter...

- mEval handles primitive special forms (lambda, if, const, define, quote, etc), itself.
- Note that, for these forms, we must use normal-order evaluation.
- For other expressions, mEval evaluates all arguments and calls mApply to perform the required operation:

### 27 A Metacircular Interpreter...

## 28 A Metacircular Interpreter...

• mapply checks if the operation is one of the builtin primitive ones, and if so performs the required operation:

```
(define (mApply Op Args)
  (case Op
        [(car) (caar Args)]
        [(cdr) (cdar Args)]
        [(cons) (cons (car Args) (cadr Args))]
        [(eq?) (eq? (car Args) (cadr Args))]
        [(null?) (null? (car Args))]
        [(+) (+ (car Args) (cadr Args))]
        [(*) (* (car Args) (cadr Args))]
        ]
        [(*) (* (car Args) (cadr Args))]
        )
)
```

## 29 A Metacircular Interpreter...

• Some auxiliary functions:

## 30 A Metacircular Interpreter...

• Note that this little interpreter lacks many of Scheme's functions.

- We don't have symbols, lambda, define.
- We can't define or invoke user-defined functions.
- There are no way to define or lookup variables, local or global. To do that, mEval and mApply pass around *environments* (association lists) of variable/value pairs.

## 31 Readings and References

• Read Scott, pp. 592–606, 609-610